

Interpreter and Transpiler for simple expressions on Nvidia GPUs using Julia

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Declaration

I hereby declare and confirm that this thesis is entirely the result of my own original work. Where other sources of information have been used, they have been indicated as such and properly acknowledged. I further declare that this or similar work has not been submitted for credit elsewhere. This printed copy is identical to the submitted electronic version.

Hagenberg, January 1, 2025

Daniel Wiplinger

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Abstract

This should be a 1-page (maximum) summary of your work in English.

Kurzfassung

An dieser Stelle steht eine Zusammenfassung der Arbeit, Umfang max. 1 Seite. ...

Chapter 1

Introduction

This chapter provides an entry point for this thesis. First the motivation of exploring this topic is presented. In addition, the research questions of this thesis are outlined. Lastly the methodology on how to answer these questions will be explained.

1.1 Background and Motivation

Optimisation and acceleration of program code is a crucial part in many fields. For example video games need optimisation to lower the minimum hardware requirements which allows more people to run the game, increasing sales. Another example where optimisation is important are computer simulations. For those, optimisation is even more crucial, as this allows the scientists to run more detailed simulations or get the simulation results faster. Equation learning is another field that can heavily benefit from optimisation. One part of equation learning, is to evaluate the expressions generated by the algorithm which can make up a significant portion of the runtime of the algorithm. This thesis is concerned with optimising the evaluation part to increase the overall performance of the equation learning algorithm.

Considering the following expression $x_1 + 5 - \text{abs}(p_1) * \text{sqrt}(x_2)/10 + 2^3$ which contains simple mathematical operations as well as variables x_n and parameters p_n . This expression is one example that can be generated by the equation learning algorithm and needs to be evaluated for the next iteration. Usually multiple expressions are generated per iteration, which also need to be evaluated. Additionally, multiple different values need to be inserted for all variables and parameters, drastically increasing the amount of evaluations that need to be performed.

The free lunch theorem as described by Adam et al. (2019) states that to gain additional performance, a developer cannot just hope for future hardware to be faster, especially on a single core. Therefore, algorithms need to utilise the other cores on a processor to further acceleration. While this approach means more development overhead, a much greater speed-up can be achieved. However, in some cases the speed-up achieved by this is still not large enough and another approach is needed. One of these approaches is the utilisation of a Graphics Processing Unit (GPU) as an easy and affordable option as compared to compute clusters. Michalakes and Vachharajani (2008) have shown a noticeable speed-up when using the GPU for weather simulation. In ad-

dition to computer simulations GPU acceleration also can be found in other places like networking (S. Han et al., 2010) or structural analysis of buildings (Georgescu et al., 2013).

1.2 Research Question

With these successful implementations of GPU acceleration, this thesis also attempts to improve the performance of evaluating mathematical equations using GPUs. Therefore, the following research questions are formulated:

- How can simple arithmetic expressions that are generated at runtime be efficiently evaluated on graphics cards?
- Under what circumstances is the evaluation of simple arithmetic expressions faster on a graphics card than on a CPU?
- Under which circumstances is the interpretation of the expressions on the GPU or the translation to the intermediate language Parallel Thread Execution (PTX) more efficient?

Answering the first question is necessary to ensure the approach of this thesis is actually feasible. If it is feasible, it is important to evaluate if evaluating the expressions on the GPU actually improves the performance over a parallelised CPU evaluator. To answer if the GPU evaluator is faster than the CPU evaluator, the last research question is important. As there are two major ways of implementing an evaluator on the GPU, they need to be implemented and evaluated to finally state if evaluating expressions on the GPU is faster and if so, which type of implementation results in the best performance.

1.3 Methodology

In order to answer the research questions, this thesis is divided into the following chapters:

Chapter 2: Fundamentals and Related Work

In this chapter, the topic of this thesis is explored. It covers the fundamentals of equation learning and how this thesis fits into this field of research. In addition, the fundamentals of General Purpose GPU computing and how interpreters and transpilers work are explained. Previous research already done within this topic is also explored.

Chapter 3: Concept and Design

Within this chapter, the concepts of implementing the GPU interpreter and transpiler are explained. How these two prototypes can be implemented disregarding concrete technologies is part of this chapter.

Chapter 4: Implementation

This chapter explains the implementation of the GPU interpreter and transpiler. The details of the implementation with the used technologies are covered, such as the interpretation process and the transpilation of the expressions into Parallel Thread Execution (PTX) code.

Chapter 5: Evaluation

The software and hardware requirements and the evaluation environment are introduced in this chapter. Furthermore, the results of the comparison of the GPU and CPU evaluators are presented to show which of these yields the best performance.

Chapter 6: Conclusion

In the final chapter, the entire work is summarised. A brief overview of the implementation as well as the evaluation results will be provided. Additionally, an outlook of possible future research is given.

With this structure the process of creating and evaluating a basic interpreter on the GPU as well as a transpiler for creating PTX code is outlined. Research is done to ensure the implementations are relevant and not outdated. Finally, the evaluation results will answer the research questions and determine if expressions generated at runtime can be evaluated more efficiently on the GPU than on the CPU.

Chapter 2

Fundamentals and Related Work

The goal of this chapter is to provide an overview of equation learning to establish common knowledge of the topic and problem this thesis is trying to solve. The main part of this chapter is split into two parts. The first part is exploring research that has been done in the field of general purpose computations on the GPU (GPGPU) as well as the fundamentals of it. Focus lies on exploring how graphics processing units (GPUs) are used to achieve substantial speed-ups and when they can be effectively employed. The second part describes the basics of how interpreters and compilers are built and how they can be adapted to the workflow of programming GPUs.

2.1 Equation learning

Equation learning is a field of research that aims at understanding and discovering equations from a set of data from various fields like mathematics and physics. Data is usually much more abundant while models often are elusive. Because of this, generating equations with a computer can more easily lead to discovering equations that describe the observed data. Brunton et al. (2016) describe an algorithm that leverages equation learning to discover equations for physical systems. A more literal interpretation of equation learning is demonstrated by Pfahler and Morik (2020). They use machine learning to learn the form of equations. Their aim was to simplify the discovery of relevant publications by the equations they use and not by technical terms, as they may differ by the field of research. However, this kind of equation learning is not relevant for this thesis.

Symbolic regression is a subset of equation learning, that specialises more towards discovering mathematical equations. A lot of research is done in this field. Keijzer (2004) and Korn (2011) presented ways of improving the quality of symbolic regression algorithms, making symbolic regression more feasible for problem-solving. Additionally, Jin et al. (2020) proposed an alternative to genetic programming (GP) for the use in symbolic regression. Their approach increased the quality of the results noticeably compared to GP alternatives. The first two approaches are more concerned with the quality of the output, while the third is also concerned with interpretability and reducing memory consumption. Bartlett et al. (2024) also describe an approach to generate simpler and higher quality equations while being faster than GP algorithms. Heuristics like GP or

neural networks as used by Werner et al. (2021) in their equation learner can help with finding good solutions faster, accelerating scientific progress. As seen by these publications, increasing the quality of generated equations but also increasing the speed of finding these equations is a central part in symbolic regression and equation learning in general. This means research in improving the computational performance of these algorithms is desired.

The expressions generated by an equation learning algorithm can look like this $x_1 + 5 - \text{abs}(p_1) * \text{sqrt}(x_2) / 10 + 2^3$. They consist of several unary and binary operators but also of constants, variables and parameters and expressions mostly differ in length and the kind of terms in the expressions. Per iteration many of these expressions are generated and in addition, matrices of values for the variables and parameters are also created. One row of the variable matrix corresponds to one instantiation of all expressions and this matrix contains multiple rows. This leads to a drastic increase of instantiated expressions that need to be evaluated. Parameters are a bit simpler, as they can be treated as constants for one iteration but can have a different value on another iteration. This means that parameters do not increase the number of expressions that need to be evaluated. However, the increase in evaluations introduced by the variables is still drastic and therefore increases the algorithm runtime significantly.

2.2 General Purpose Computation on Graphics Processing Units

Graphics cards (GPUs) are commonly used to increase the performance of many different applications. Originally they were designed to improve performance and visual quality in games. Dokken et al. (2005) first described the usage of GPUs for general purpose programming. They have shown how the graphics pipeline can be used for GPGPU programming. Because this approach also requires the programmer to understand the graphics terminology, this was not a great solution. Therefore, Nvidia released CUDA¹ in 2007 with the goal of allowing developers to program GPUs independent of the graphics pipeline and terminology. A study of the programmability of GPUs with CUDA and the resulting performance has been conducted by Huang et al. (2008). They found that GPGPU programming has potential, even for non-embarassingly parallel problems. Research is also done in making the low level CUDA development simpler. T. D. Han and Abdelrahman (2011) have described a directive-based language to make development simpler and less error-prone, while retaining the performance of handwritten code. To drastically simplify CUDA development Besard, Foket, et al. (2019) showed that it is possible to develop with CUDA in the high level programming language Julia² while performing similar to CUDA written in C. In a subsequent study Lin and McIntosh-Smith (2021) found that high performance computing (HPC) on the CPU and GPU in Julia performs similar to HPC development in C. This means that Julia can be a viable alternative to Fortran, C and C++ in the HPC field and has the additional benefit of developer comfort since it is a high level language with modern features such as garbage-collectors. Besard, Churavy, et al. (2019) have also shown how the combination of Julia and CUDA help in rapidly developing HPC software. While this

¹<https://developer.nvidia.com/cuda-toolkit>

²<https://julialang.org/>

thesis in general revolves around CUDA, there also exist alternatives by AMD called ROCm³ and a vendor independent alternative called OpenCL⁴.

While in the early days of GPGPU programming a lot of research has been done to assess if this approach is feasible, it now seems obvious to use GPUs to accelerate algorithms. Weather simulations began using GPUs very early for their models. In 2008 Michalakes and Vachharajani (2008) proposed a method for simulating weather with the WRF model on a GPU. With their approach, they reached a speed-up of the most compute intensive task of 5 to 20, with very little GPU optimisation effort. They also found that the GPU usages was very low, meaning there are resources and potential for more detailed simulations. Generally, simulations are great candidates for using GPUs, as they can benefit heavily from a high degree of parallelism and data throughput. Köster et al. (2020) have developed a way of using adaptive time steps to improve the performance of time step simulations, while retaining their precision and constraint correctness. Black hole simulations are crucial for science and education for a better understanding of our world. Verbraeck and Eisemann (2021) have shown that simulating complex Kerr (rotating) black holes can be done on consumer hardware in a few seconds. Schwarzschild black hole simulations can be performed in real-time with GPUs as described by Hissbach et al. (2022) which is especially helpful for educational scenarios. While both approaches do not have the same accuracy as detailed simulations on supercomputers, they show how single GPUs can yield similar accuracy at a fraction of the cost. Networking can also heavily benefit from GPU acceleration as shown by S. Han et al. (2010), where they achieved a significant increase in throughput than with a CPU only implementation. Finite element structural analysis is an essential tool for many branches of engineering and can also heavily benefit from the usage of GPUs as demonstrated by Georgescu et al. (2013). However, it also needs to be noted, that GPUs are not always better performing than CPUs as illustrated by Lee et al. (2010), but they still can lead to performance improvements nonetheless.

2.2.1 Programming GPUs

The development process on a GPU is vastly different from a CPU. A CPU has tens or hundreds of complex cores with the AMD Epyc 9965⁵ having a staggering 192 cores and twice as many threads. A guide for a simple one core 8-bit CPU has been published by Schuurman (2013). He describes the many different and complex parts of a CPU core. Modern CPUs are even more complex, with dedicated fast integer, floating-point arithmetic gates as well as logic gates, sophisticated branch prediction and much more. This makes a CPU perfect for handling complex control flows on a single program strand and on modern CPUs even multiple strands simultaneously. However, as seen in section 2.2, this often isn't enough. On the other hand, a GPU contains thousands or even tens of thousands of cores. For example, the GeForce RTX 5090⁶ contains a total of 21760 CUDA cores. To achieve this enormous core count a single GPU core has to be much simpler than one CPU core. As described by Nvidia (2024) a GPU designates

³<https://www.amd.com/de/products/software/rocm.html>

⁴<https://www.khronos.org/opencl/>

⁵<https://www.amd.com/en/products/processors/server/epyc/9005-series/amd-epyc-9965.html>

⁶<https://www.nvidia.com/en-us/geforce/graphics-cards/50-series/rtx-5090/>

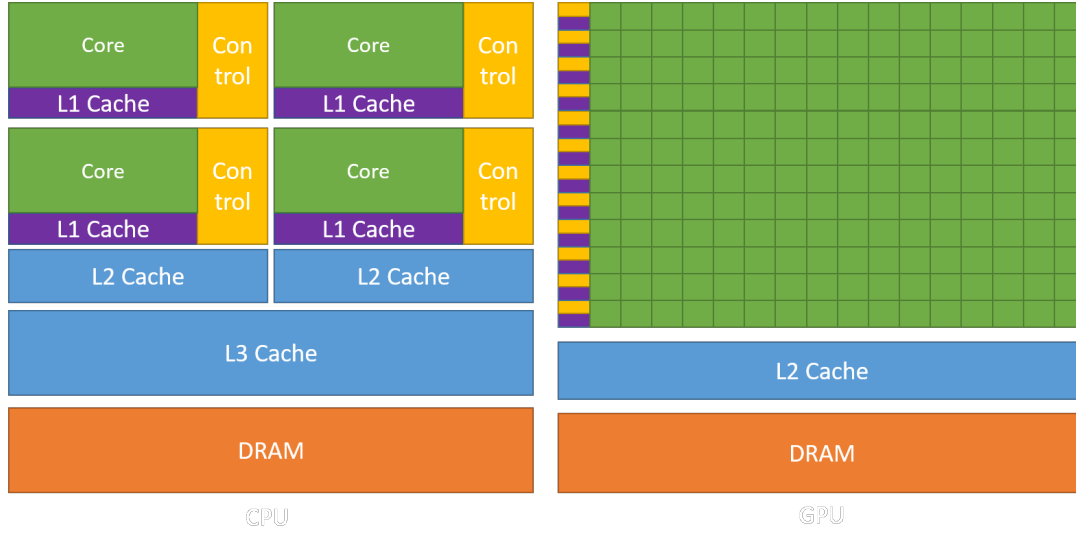


Figure 2.1: Overview of the architecture of a CPU (left) and a GPU (right). Note the higher number of simpler cores on the GPU (Nvidia, 2024).

much more transistors towards floating-point computations. This results in less efficient integer arithmetic and control flow handling. There is also less Cache available per core and clock speeds are usually also much lower than those on a CPU. An overview of the differences of a CPU and a GPU architecture can be seen in figure 2.1.

Despite these drawbacks, the sheer number of cores, makes a GPU a valid choice when considering improving the performance of an algorithm. Because of the high number of cores, GPUs are best suited for data parallel scenarios. This is due to the SIMD architecture of these cards. SIMD stands for Single-Instruction Multiple-Data and states that there is a single stream of instructions that is executed on a huge number of data streams. Franchetti et al. (2005) and Tian et al. (2012) describe ways of using SIMD instructions on the CPU. Their approaches lead to noticeable speed-ups of 3.3 and 4.7 respectively by using SIMD instructions instead of serial computations. Extending this to GPUs which are specifically built for SIMD/data parallel calculations shows why they are so powerful despite having less complex and slower cores than a CPU.

While the concepts of GPGPU programming are the same no matter the GPU used, the naming on AMD GPUs and guides differs from the CUDA naming. As previously stated, this thesis will use the terminology and concepts as described by Nvidia in their CUDA programming guide.

The many cores on a GPU, also called threads, are grouped together in several categories. On the lowest level exists a streaming multiprocessor (SM) which is a hardware unit responsible for scheduling and executing threads and also contains the registers used by the threads. One SM is always executing a group of 32 threads simultaneously and this group is called a warp. The number of threads that can be started is virtually unlimited. However, threads need to be grouped in a block, with one block usually containing a maximum of 1024 threads. Therefore, if more than 1024 threads are needed, more blocks need to be created. All threads in one block have access to some shared

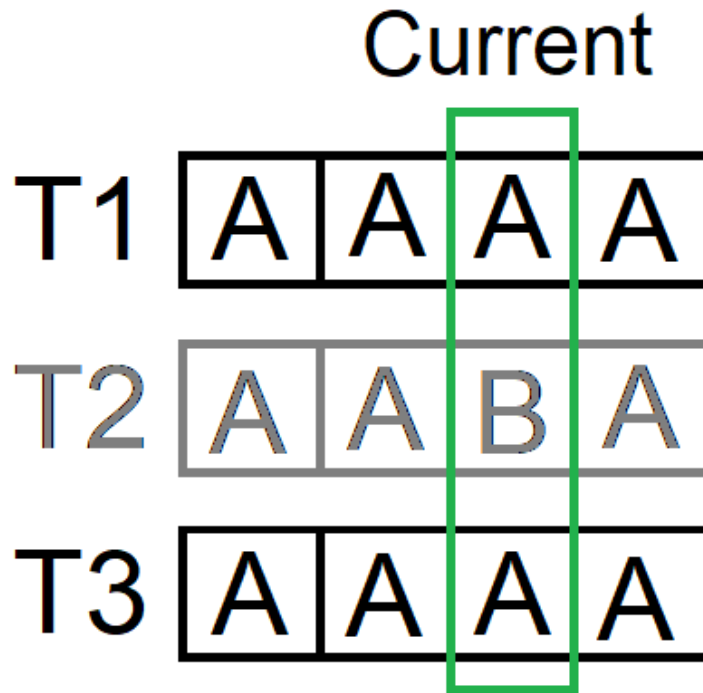


Figure 2.2: Thread T2 wants to execute instruction B while T1 and T3 want to execute instruction A. Therefore T2 will be an inactive thread this cycle and active once T1 and T3 are finished. This means that now the divergent threads are serialised.

memory, which can be used for L1-caching or communication between threads. It is important that the blocks can be scheduled independently from on another with no dependencies between them. This allows the scheduler to schedule blocks and threads as efficiently as possible. All threads within a warp are ensured to be part of the same block and therefore executed simultaneously (Nvidia, 2024).

While all threads in a warp start at the same point in a program, they have their own instruction address, allowing them to work independently. Because of the SIMD architecture, all threads in a warp must execute the same instructions and if threads start diverging, the SM must pause threads with different instructions and execute them later. Figure 2.2 shows how such divergences can impact performance. The situation described by the figure also shows, that after the divergent thread would reconverge, this does not happen and leads to T2 being executed after T1 and T3 are finished. In situations where a lot of data dependent thread divergence happens, most of the benefits of using a GPU have vanished.

Threads not executing the same instruction is against the SIMD principle but can happen in reality, due to data dependent branching. Consequently, this leads to bad resource utilisation, which in turn leads to worse performance. Another possibility of threads being paused (inactive threads) is the fact that sometimes, the number of threads started is not divisible by 32. In such cases, the last warp still contains 32

threads but only the threads with work are executed (Nvidia, 2024).

Modern GPUs implement the so called Single-Instruction Multiple-Thread (SIMT) architecture. In many cases a developer does not need to know the details of SIMT and can develop fast and correct programs with just the SIMD architecture in mind. However, leveraging the power of SIMT can yield substantial performance gains by re-converging threads once data dependent divergence occurred. A proposal for a re-convergence algorithm was proposed by Collange (2011) where they have shown that these approaches help with hardware occupation, resulting in improved performance as threads are now no longer fully serialised. Another approach for increasing occupancy using the SIMT architecture is proposed by Fung and Aamodt (2011). They introduced a technique for compacting thread blocks by moving divergent threads to new warps until they reconverge. This approach resulted in a noticeable speed-up between 17% and 22%.

Talk about memory allocation (with the one paper diving into dynamic allocations)
Memory transfer (with streams potentially)

2.2.2 Parallel Thread Execution

Describe what PTX is to get a common ground for the implementation chapter. Probably a short section

2.3 Compilers

Maybe even move this entire section to “Concept and Design”?

brief overview about compilers (just setting the stage for the subsections basically).
Talk about register management and these things.

2.3.1 Interpreters

What are interpreters; how they work; should mostly contain/reference gpu interpreters

2.3.2 Transpilers

talk about what transpilers are and how to implement them. If possible also gpu specific transpilation.

Chapter 3

Concept and Design

introduction to what needs to be done. also clarify terms “Host” and “Device” here

3.1 Requirements and Data

short section. Multiple expressions; vars for all expressions; params unique to expression; operators that need to be supported

3.2 Interpreter

as introduction to this section talk about what “interpreter” means in this context. so “gpu parses expr and calculates”

3.2.1 Architecture

talk about the coarse grained architecture on how the interpreter will work. (.5 to 1 page probably)

3.2.2 Host

talk about the steps taken to prepare for GPU interpretation

3.2.3 Device

talk about how the actual interpreter will be implemented

3.3 Transpiler

as introduction to this section talk about what “transpiler” means in this context. so “cpu takes expressions and generates ptx for gpu execution”

3.3.1 Architecture

talk about the coarse grained architecture on how the transpiler will work. (.5 to 1 page probably)

3.3.2 Host

talk about how the transpiler is implemented

3.3.3 Device

talk about what the GPU does. short section since the gpu does not do much

Chapter 4

Implementation

4.1 Technologies

Short section; CUDA, PTX, Julia, CUDA.jl

Probably reference the performance evaluation papers for Julia and CUDA.jl

4.2 Interpreter

Talk about how the interpreter has been developed.

4.3 Transpiler

Talk about how the transpiler has been developed

Chapter 5

Evaluation

5.1 Test environment

Explain the hardware used, as well as the actual data (how many expressions, variables etc.)

5.2 Results

talk about what we will see now (results only for interpreter, then transpiler and then compared with each other and a CPU interpreter)

5.2.1 Interpreter

Results only for Interpreter

5.2.2 Transpiler

Results only for Transpiler

5.2.3 Comparison

Comparison of Interpreter and Transpiler as well as Comparing the two with CPU interpreter

Chapter 6

Conclusion and Future Work

Summarise the results

6.1 Future Work

talk about what can be improved

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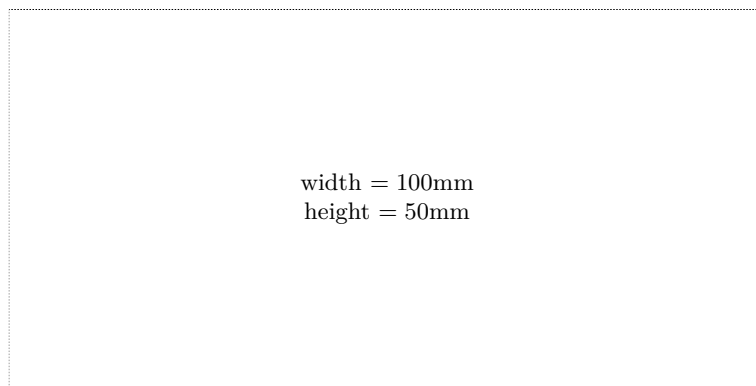
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